

**Exercise series N°03**

**Exercise 1:** choose the correct answer for the following questions

1. **What is the primary difference between a probit model and a logit model?**
  - a) The probit model uses the logistic function, while the logit model uses the normal cumulative distribution function (CDF).
  - b) The probit model assumes a normal distribution of errors, whereas the logit model assumes a logistic distribution of errors.
  - c) The probit model is used for linear regression, while the logit model is used for classification.
  - d) There is no fundamental difference between the two models.
2. **In a probit model, what type of function links the independent variables to the probability of an event occurring?**
  - a) Linear function
  - b) Logarithmic function
  - c) Normal cumulative distribution function (CDF)
  - d) Exponential function
3. **Which of the following is an assumption of the probit model?**
  - a) The error terms follow a standard normal distribution.
  - b) The dependent variable must be continuous.
  - c) The independent variables must be normally distributed.
  - d) The dependent variable must have more than two categories.
4. **If the estimated coefficient in a probit model is positive, what does it imply?**
  - a) The probability of the event occurring decreases.
  - b) The probability of the event occurring increases.
  - c) The variable is not significant.
  - d) The direction of the effect cannot be determined.
5. **If a probit model is estimated as follows:  $P(Y=1|X)=\Phi(0.5+1.5X)$**

**What is the probability of  $Y=1$  when  $X=1$ ?**

- a) 0.9772
- b) 0.5000
- c) 0.0228
- d) 0.7500

6. Which of the following is a common issue when interpreting probit model coefficients?
  - a) The coefficients directly represent the change in probability.
  - b) The coefficients do not have a direct probabilistic interpretation.
  - c) The coefficients can be interpreted in the same way as those in a linear regression model.
  - d) The coefficients are always positive.
7. Which test is commonly used to assess the overall goodness-of-fit of a probit model?
  - a) Durbin-Watson test
  - b) Wald test
  - c) Hosmer-Lemeshow test
  - d) McFadden's  $R^2$
8. Which of the following distributions does the probit model assume for the error term?
  - a) Standard normal distribution
  - b) Exponential distribution
  - c) Logistic distribution
  - d) Poisson distribution
9. You estimate a probit model and find the following output: Intercept: -1.2 , Coefficient on X: 2.4

What is the probability of  $Y=1$  when  $X=1.0$ ?

- a) 0.8849
  - b) 0.1151
  - c) 0.5000
  - d) 0.7500
10. A probit model estimates  $P(Y=1|X)=\Phi(2.3X-1.1)$ . If  $X=0.8$ , what is the probability of  $Y=1$ ?
  - a) 0.7704
  - b) 0.2296
  - c) 0.5000
11. In a probit model, a coefficient of -0.7 for an independent variable means:
  - a) The probability decreases, but the change depends on the standard normal distribution.
  - b) The probability decreases by exactly 0.7 for every unit increase in the variable.
  - c) The probability decreases by 70%.
  - d) The probability is always negative.
12. If  $\beta_3=-0.4$  and  $X_3$  increases from 1 to 2, what happens to the probability of the event occurring?
  - a) It increases
  - b) It decreases
  - c) It stays the same
  - d) It becomes exactly 0.5000

**13. A researcher estimates a probit model with the following equation:**

$$Z = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \beta_3 X_3$$

where:  $\beta_0 = -0.8$ ,  $\beta_1 = 1.2$ ,  $\beta_2 = 0.5$ ,  $\beta_3 = -0.4$

If  $X_1 = 2$ ,  $X_2 = 3$ , and  $X_3 = 1$ , what is the predicted **Z-score** and the probability of event occurring?

- a) z-score is 2.1, the probability is 0.9821
- b) z-score is 1.8, the probability is 0.9641
- c) z-score is 2.1, the probability is 0.9820
- d) z-score is 1.8, the probability is 0.9821

**Exercise 2**

A bank wants to predict whether a loan applicant will default on their loan based on: **Credit Score (X1)** and **Loan Amount (X2)**

Credit Score (X1)	Loan Amount	Default
600	30	1
650	25	1
700	15	1
750	10	0
720	12	0
680	20	1
710	18	1
640	28	1
670	22	1
730	14	1
690	19	1
620	27	1
740	13	0
660	24	1
780	9	0
630	26	1
760	11	1
725	17	0
605	31	1
675	23	1
745	12	1
695	21	0
715	16	0
655	29	1
785	8	1
610	32	1
770	10	0

725	18	0
640	30	1
720	14	0

1. Write the Probit model equation to predict the probability of loan default ;
2. Estimate the parameters, interpret the results;
3. If a borrower has a **Credit Score of 650** and a **Loan Amount of \$25,000\$**, what is the predicted Z-score
4. Predict Default for a New Applicant, who has: **Credit Score =800, Loan Amount = \$15,000\$**
5. If an applicant **increases** their loan amount from **\$10,000\$ to \$20,000\$**, and the coefficient for Loan what happens to the predicted Z-score?
6. If a **Credit Score = 750** and a **Loan Amount = \$10,000\$**, what is the predicted **Z-score** and probability of default? (Use  $\Phi(-0.3) = 0.3821$ )