

Travaux Dirigés (Série n°3)

**Exercise N° 1 :**

The stress state at point P of a material is given by the tensor defined in the basis  $(e_1, e_2, e_3)$ . Its representative matrix is :

$$\Sigma = \begin{pmatrix} 7 & 0 & 5 \\ 0 & 12 & 0 \\ 5 & 0 & 9 \end{pmatrix} \text{ daN/mm}^2$$

- 1°) Determine the principal stress and principal directions of  $\Sigma$  in P.
- 2°) Determine the spherical and deviatoric stress tensors for this stress state.
- 3°) Determine the components  $\sigma$  and  $\tau$  of the stress vector in the direction of the first bisector of the plane  $(e_1, e_3)$ .

**Exercise N° 2 :**

The state of stress at point P is given with respect to basis  $(e_1, e_2, e_3)$  by the following matrix :

$$\Sigma_p = \begin{pmatrix} 0.7 & 3.6 & 0 \\ 3.6 & 2.8 & 0 \\ 0 & 0 & 7.6 \end{pmatrix} \text{ (daN/mm}^2\text{)}$$

- 1°) Determine the principal stress and principal directions of  $\Sigma$  in P.
- 2°) Calculate the components of the stress applied at point P, on the facet whose normal has the direction cosine of  $(\sqrt{3}/2, 1/2, 0)$ .
- 3°) Decompose the stress tensor  $\Sigma$  into a spherical part and a deviatoric part.

**Exercise N°03 :**

Let, at point P of a material, be the stress tensor defined in the basis  $(e_1, e_2, e_3)$ . Its representative matrix is :

$$\Sigma = \begin{pmatrix} 4 & k & k \\ k & 7 & 2 \\ k & 2 & 4 \end{pmatrix} \text{ daN/mm}^2 \quad \text{where } k \text{ is a real number; } \sigma_{III} = 3 \text{ daN/mm}^2 \text{ et } \sigma_I = 2\sigma_{II}$$

- 1°) Determine the principal stress of  $\Sigma$  in P.
- 2°) Determine the value of k.
- 3°) Decompose the stress tensor  $\Sigma$  into a spherical part and a deviatoric part.
- 4°) Determine octahedral tension and shear.