

Tutorials 3

Exercise 1:

In a Cartesian coordinate system (O, x, y), equipped with the basis vectors (\vec{i}, \vec{j}) a moving point M has parametric equations: $X=2\cos(3t+2)$ et $Y = 2\sin(3t+2)$

1. Give the equation of the trajectory, what is its nature?
2. Express the velocity vector \vec{V} , and determine its magnitude (modulus).
3. Give the acceleration vector \vec{a} , and determine its magnitude (modulus).
4. Give the Polar coordinates of point M.
5. Give the position, velocity and acceleration vectors in polar coordinates.

Exercise 2:

Consider a mobile M treated as a material point moving in the XOY plane. It is identified by its polar coordinates: $r(t) = t^2/4$; $\theta(t) = \frac{\pi}{4}t$ (t in s. r in m et θ in rd).

- 1/ Express the position, velocity and acceleration vectors in polar coordinates.
- 2/ Calculate the magnitude (modulus) of the velocity vector and acceleration vector at t=6s.
- 3/ Give the Cartesian coordinates of point M.
- 4/ Deduce the expression of the velocity vector in Cartesian coordinates.

Exercise 3:

A mobile point M follows a plane trajectory given by the equations in polar coordinates ($0, \vec{e}_r, \vec{e}_\theta$)

$$\begin{cases} r(t) = e^t \\ \theta(t) = t \end{cases} \quad (t \text{ in s, } r \text{ in met } \theta \text{ in rad})$$

1. Express $(\vec{e}_r, \vec{e}_\theta)$ in terms of fixed basis (\vec{i}, \vec{j}).
2. Express the position vector \overline{OM} in polar coordinates.
3. Calculate the velocity vector \vec{V} , and determine its magnitude (modulus).
4. Calculate the acceleration vector a, and determine its magnitude (modulus).
5. Deduce the position vector \overline{OM} in Cartesian coordinates.