## Mathematical recall and vector operations

## Problem 1:

The forces $\mathbf{F}_{1}, \mathbf{F}_{2}$, and $\mathbf{F}_{3}$, all of which act on point $A$ of the bracket, are specified in three different ways (Fig.1).

- Determine the $x$ and $y$ scalar components of each of the three forces.


## Problem 2:



Combine the two forces $\mathbf{P}$ and $\mathbf{T}$, which act on the fixed structure at $B$, into a single equivalent force $\mathbf{R}$ (Fig.2).

## Problem 3:

Forces $\mathbf{F}_{1}$ and $\mathbf{F}_{2}$ act on the bracket as shown in (Fig.3). Determine:
1- The magnitude of the resultant force $\mathbf{R}$.


2- The projection $F_{b}$ of their resultant $\mathbf{R}$ onto the $b$-axis.

## Problem 4:

If the force $\mathbf{F}$ has a magnitude of 1200 N and angle $\theta_{x}$ is $60^{\circ}$ and $\theta_{y}$ is $45^{\circ}$ (Fig.4).
1- Express the force in Cartesian form.


2- Determine its unit vector.

## Problem 5:

If the coordinate direction angles $\theta_{x}=112^{\circ}, \theta_{y}=75^{\circ}$ and $\mathrm{F}_{z}=5 \mathrm{~cm}$ (Fig.4).

- Determine the magnitude of vector $\mathbf{F}$.


## Problem 6:

A force $\mathbf{F}$ with a magnitude of 100 N is applied at the origin $O$ of the axes $x-y-z$ as shown in (Fig.5). The line of action of $\mathbf{F}$ passes through a point $A$ whose coordinates are $3 \mathrm{~m}, 4 \mathrm{~m}$, and 5 m . Determine:

1- The $x, y$, and $z$ scalar components of $\mathbf{F}$,
2- The projection $\mathrm{F}_{x y}$ of $\mathbf{F}$ on the $x-y$ plane,
3- The projection $\mathrm{F}_{O B}$ of $\mathbf{F}$ along the line $O B$ using dot product.


