

# Chapitre IV

## Caractéristiques géométriques des sections

### I-1 Moment statique

$$S_y = \iint_A z' \, dA \quad [m^3]$$

$$S_{z'} = \iint_A y \, dA$$

$$S_{yG} = 0 \quad \text{et} \quad S_{zG} = 0$$

### I-2 Position du centre de gravité

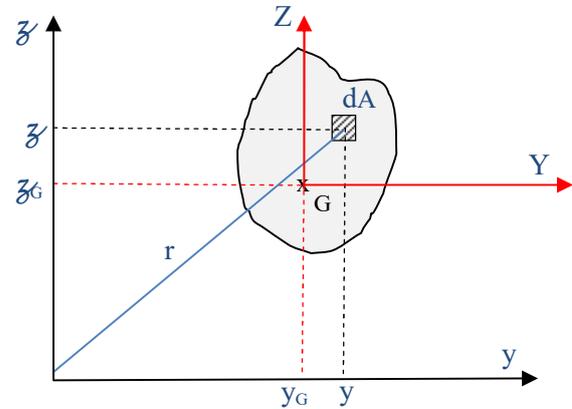
$$y_G = \frac{1}{A} \iint_A y \, dA = \frac{S_{z'}}{A} \quad [m]$$

$$z'_G = \frac{1}{A} \iint_A z' \, dA = \frac{S_y}{A}$$

donc :

$$S_y = A \cdot z'_G$$

$$S_{z'} = A \cdot y_G$$



Dans le cas de sections composées :

$$S_y = \sum A_i \cdot z'_{Gi}$$

$$S_{z'} = \sum A_i \cdot y_{Gi}$$

### I-3 Moment d'inertie quadratique

$$I_y = \iint_A z'^2 \, dA \quad [m^4]$$

$$I_{z'} = \iint_A y^2 \, dA$$

### I-4 Moment d'inertie polaire

$$I_p = \iint_A r^2 \, dA = \iint_A (y^2 + z'^2) \, dA = I_{z'} + I_y \quad [m^4]$$

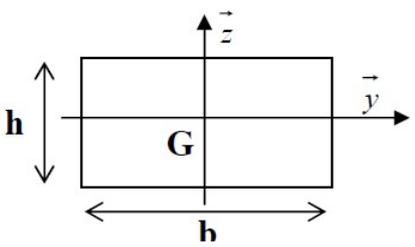
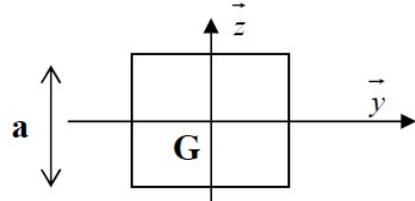
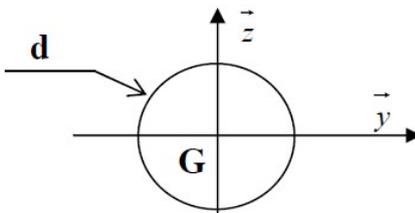
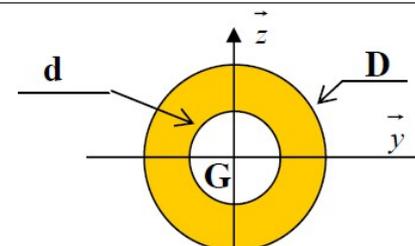
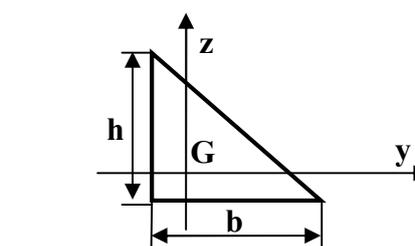
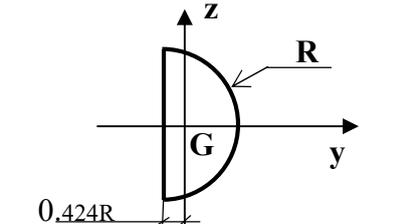
### I-5 Produit d'inertie

$$I_{yz'} = \iint_A y z' \, dA \quad [m^4]$$

### I-6 Moment d'inertie par rapport aux axes parallèles (théorème de Huygens)

$$\begin{aligned} z' &= z'_G + Z \\ y &= y_G + Y \end{aligned} \quad \implies \quad \begin{aligned} I_y &= I_{yG} + z_G^2 \cdot A \\ I_{z'} &= I_{zG} + y_G^2 \cdot A \\ I_{yz'} &= I_{YZG} + y_G z'_G \cdot A \end{aligned}$$

**Moment d'inertie quadratique de sections usuelles**

	$I_{Gyy}$	$I_{Gzz}$	$I_G = I_{Gyy} + I_{Gzz}$
	$\frac{b.h^3}{12}$	$\frac{h.b^3}{12}$	$\frac{hb}{12}(b^2+h^2)$
	$\frac{a^4}{12}$	$\frac{a^4}{12}$	$\frac{a^4}{6}$
	$\frac{\pi.d^4}{64}$	$\frac{\pi.d^4}{64}$	$\frac{\pi.d^4}{32}$
	$\frac{\pi}{64}(D^4-d^4)$	$\frac{\pi}{64}(D^4-d^4)$	$\frac{\pi}{32}(D^4-d^4)$
	$\frac{bh^3}{36}$	$\frac{hb^3}{36}$	$\frac{bh(h^2 + b^2)}{36}$
	$0.39 R^4$	$0.11 R^4$	$0.50 R^4$