

## TD4: (الحل) المكاملة

التمرين الأول:

1.  $\frac{1}{5}x^5 + 3\cos x + \frac{4}{3}x^{3/2} + c$

2.  $\tan x + c$

3.  $-\arcsin x + c$

التمرين الثاني:

1.  $\ln|+3x + 4| + c$

2.  $\frac{1}{3}\cos^3 x - \cos x + c$

3.  $\frac{1}{2}\arctan \frac{x}{2} + c$

4.  $\frac{1}{3}\sin^3 x - \frac{1}{5}\sin^5 x + c$

5.  $\frac{1}{4}(\arctan x)^4 + c$

6.  $x - \ln(1 + x + c)$

التمرين الثالث:

1.  $x\arctan x - \frac{1}{2}\ln(1 + x^2) + c$

2.  $\frac{1}{2}x^2 \ln x - \frac{1}{4}x^2 + c$

3.  $\frac{1}{2}e^x(\sin x - \cos x) + c$

4.  $x - (\arcsin x)\sqrt{1 - x^2} + c$

5.  $\frac{1}{8}\sin 2x - \frac{1}{4}x\cos 2x + c$

التمرين الرابع:

$$\frac{1}{2} \ln \left| \frac{x-1}{x+1} \right| + c .1$$

$$\ln|x| - \frac{1}{2} \ln(1 + x^2) + c .2$$

$$\frac{1}{3} x^3 + x + \frac{1}{2} \ln \left| \frac{x-1}{x+1} \right| + c .3$$

$$\frac{1}{3} \ln|x - 1| - \frac{1}{6} \ln(x^2 + x + 1) - \frac{1}{\sqrt{3}} \arctan \frac{2x+1}{\sqrt{3}} + c .4$$

التمرين الخامس:

$$(\arctan x - \arcsin x) \Big|_0^1 = -\frac{\pi}{4} .1$$

$$(-\ln|\cos x|) \Big|_0^{\pi/3} = \ln 2 .2$$

$$(-\arctan(\cos x)) \Big|_0^{\pi} = \frac{\pi}{2} .3$$

$$\left( \frac{1}{4} \ln^4 x \right) \Big|_1^e = \frac{1}{4} .4$$